

Empirical Time-Dimension Model of Spectrum Use based on Discrete-Time Markov Chain with Deterministic and Stochastic Duty Cycle Models

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Abstract—The spectrum occupancy models widely used to the date in Dynamic Spectrum Access/Cognitive Radio (DSA/CR) research frequently rely on assumptions and oversimplifications that have not been validated with empirical measurement data. In this context, this work presents an empirical time-dimension model of spectrum use appropriate for DSA/CR studies. Concretely, a discrete-time two-state Markov chain with novel deterministic and stochastic duty cycle models is proposed as an adequate mean to accurately describe spectrum occupancy in the time domain. The validity and accuracy of the proposed modeling approach is evaluated and corroborated with extensive empirical data from a multi-band spectrum measurement campaign. The obtained results demonstrate that the proposed approach is able to accurately capture and reproduce the relevant statistical properties of spectrum use observed in real-world channels of various radio technologies. The importance of accurately modeling spectrum use in the design and evaluation of novel DSA/CR techniques is highlighted with a practical case study.

Index Terms—Cognitive radio, dynamic spectrum access, spectrum usage models, time dimension.

I. INTRODUCTION

THE owned spectrum allocation policy, in use since the early days of modern radio communications, assigns fixed spectrum bands to particular wireless standards. Such bands are further divided into sub-bands that are allocated under static licenses and remain solely for the exclusive use of the licensee. This allocation policy has been proven to effectively control interference among radio communication systems and simplify the design of hardware for use at a known and fixed range of frequencies. However, the overwhelming proliferation of new operators, innovative services and wireless technologies during the last years has resulted, under this static regulatory regime, in the depletion of all spectrum bands with commercially attractive radio propagation characteristics. The vast majority of spectrum regarded as usable has already been allocated, thus hindering the commercial rollout of new emerging services.

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An important number of spectrum measurement campaigns covering wide frequency ranges [1]–[13] as well as some specific licensed bands [14]–[20] has been carried out all over the world in order to determine the degree to which allocated spectrum bands are used in real wireless communication systems. Empirical measurements have demonstrated that spectrum is mostly underutilized, thus indicating that the virtual spectrum scarcity problem actually results from static and inflexible spectrum management policies rather than the physical scarcity of usable radio frequencies. The owned spectrum allocation policy was once appropriate, but nowadays it has become obsolete and new spectrum management paradigms are therefore required in order to efficiently exploit the precious radio resources. This situation has motivated the emergence of more flexible spectrum access policies [21]–[23]. In this context, the Dynamic Spectrum Access (DSA) principle [24], based on the Cognitive Radio (CR) paradigm [25], [26], has gained popularity as a promising solution to conciliate the existing conflicts between the ever-increasing spectrum demand growth and the currently inefficient spectrum utilization.

The basic underlying idea of DSA/CR is to allow unlicensed (secondary) users to access in an opportunistic and non-interfering manner some licensed bands temporarily unoccupied by licensed (primary) users. Unlicensed secondary terminals monitor the spectrum in order to identify time gaps left unused by primary users, usually referred to as *white spaces* or *spectrum holes* [27], place secondary transmissions within such spaces and vacate the channel as soon as primary users return. Secondary unlicensed transmissions are allowed following this operating principle as long as they do not result in harmful interference to primary radios.

Due to the opportunistic nature of the DSA/CR principle, the behavior and performance of a secondary network depends on the spectrum occupancy patterns of the primary system. A realistic and accurate modeling of such patterns becomes therefore essential and extremely useful in the domain of DSA/CR research. The potential applicability of spectrum use models ranges from analytical studies to the design and dimensioning of secondary networks, as well as the development of innovative simulation tools and more efficient DSA techniques for wireless communication systems where the DSA/CR technology can be applied, including heterogeneous wireless access systems [28] as well as vehicular networks [29]–[31]. Nevertheless, the utility of such models depends on their realism and accuracy. Unfortunately, the models for

spectrum use commonly used to the date in DSA/CR research are limited in scope and based on oversimplifications or assumptions that have not been validated with empirical measurement data. Spectrum occupancy modeling in the context of DSA/CR constitutes a rather unexplored research area that still requires more effort.

The problem of modeling spectrum occupancy in the spatial dimension was addressed in [32], [33]. This work focuses on the time domain of spectrum usage and extends previous work [34]. In particular, a discrete-time two-state Markov chain with deterministic and stochastic Duty Cycle (DC) models is proposed as an adequate mean to accurately describe spectrum occupancy in the time domain. The validity and correctness of the model developed in this work is evaluated and corroborated with extensive empirical measurement results for various frequency bands and radio technologies. The obtained results demonstrate that the proposed approach is able to capture and reproduce with significant accuracy the statistical properties of spectrum use observed in real-world channels.

The remainder of this paper is organized as follows. First, Section II reviews the existing related work on time-dimension models of spectrum use, identifying the existing deficiencies that motivate this work. Section III describes the measurement setup and methodology employed to capture the empirical data used in the validation of the proposed model. Section IV presents the traditional Markov chain model commonly used in previous literature. Since such Markov model is not able to accurately capture and reproduce all the relevant statistical properties of spectrum use in the time domain, it is extended with adequate deterministic and stochastic DC models, which are presented in Sections V and VI, respectively. The validity and accuracy of the developed model is assessed and verified in Section VII. The importance of disposing of accurate models of spectrum use, as the one presented in this work, for the design and evaluation of novel DSA/CR techniques is highlighted with a practical case study in Section VIII. Finally, Section IX summarizes the research carried out in this work.

II. RELATED WORK AND MOTIVATION

A. Previous Work based on Continuous-Time Markov Chains

From the point of view of a DSA/CR network, spectrum use can adequately be modeled by means of a Markov chain with two states, one indicating that the channel is busy (i.e., used by a primary user and therefore not available for opportunistic access) and the other one indicating that it is idle (i.e., available for secondary use). A popular channel model in DSA/CR research is the well-known two-state Continuous-Time Markov Chain (CTMC) model, where the channel remains in one state for a random time period before switching to the other state. The *state holding time* or *sojourn time* is modeled as an exponentially distributed random variable.

The CTMC model has widely been employed in the study of various aspects of DSA/CR networks such as Medium Access Control (MAC) protocols for spectrum sharing [35], [36], MAC-layer sensing schemes [37]–[39], adaptive spectrum sensing solutions [40], the sensing-throughput tradeoff [41], [42] and the performance of DSA/CR sensor networks [43].

Although the CTMC model has widely been used in the literature, some works based on empirical measurements [44]–[48] have demonstrated that state holding times are not exponentially distributed in practice. In particular, it was found that state holding times are more adequately described by means of generalized Pareto [44], a mixture of uniform and generalized Pareto [45], [46], hyper-Erlang [45], [46], generalized Pareto and hyper-exponential [47], as well as geometric and log-normal [48] distributions. Based on the conclusions from previous modeling works, a more appropriate model is therefore the Continuous-Time Semi-Markov Chain (CTSMC) model, where the state holding times can follow any arbitrary distribution. As a result, some works have considered CTSMC models. This is the case, for instance, of [49], [50], which consider a CTSMC model where the busy/idle periods are exponentially/Erlang-distributed, respectively.

B. Previous Work based on Discrete-Time Markov Chains

In the two-state Discrete-Time Markov Chain (DTMC) model the time index set is discrete. According to this model, the channel remains in a certain state at each step, with the state changing randomly between steps. The behavior of the channel is described by means of a set of transition probabilities between states.

The DTMC model has widely been used in the DSA/CR literature as well. For instance, it has been used to analyze the performance of MAC [51] and joint MAC/sensing [52] frameworks for opportunistic spectrum access, dynamic channel selection strategies [53], opportunistic scheduling policies [54], channel selection schemes [55] based on the interference temperature model [56], and the voice-service capacity of DSA/CR systems under both ideal [57] and imperfect [58] spectrum sensing conditions, as well as under quality-of-service restrictions [59].

As opposed to the continuous-time case, and to the best of the authors' knowledge, the suitability of the DTMC channel model in describing the statistical properties of spectrum occupancy patterns in real systems has not been evaluated and assessed in the literature before¹. This means that an important volume of research in DSA/CR has been based on assumptions or oversimplifications that have not been validated with empirical measurement data and, more importantly, that future research works based on the DTMC channel model will also suffer from the same drawback due to the non-existence of appropriate DTMC modeling approaches capable to capture the relevant statistical properties of spectrum occupancy in the time domain. In this context, this work covers such deficiencies and fills the existing gaps by evaluating the ability of the DTMC model to reproduce the statistical properties of spectrum use in real radio communication systems, and extending the conventional DTMC model with appropriate deterministic and stochastic DC models.

¹A DTMC model could be characterized by discrete-time distributions for state holding times instead of a set of transition probabilities between states. While the former approach has received some attention [48], the latter, which has widely been employed in the literature, remains unexplored and is studied in this work.

III. MEASUREMENT SETUP AND METHODOLOGY

The employed measurement configuration (see Figure 1) relies on a spectrum analyzer setup where different external devices have been added in order to improve the detection capabilities and hence the accuracy and reliability of measurements. The design is composed of two broadband discone-type antennas covering the frequency range from 75 to 7075 MHz, a Single-Pole Double-Throw (SPDT) switch to select the desired antenna, several filters to remove undesired overloading (FM) and out-of-band signals, a low-noise pre-amplifier to enhance the overall sensitivity and thus the ability to detect weak signals, and a high performance spectrum analyzer to record the spectral activity. The spectrum analyzer is connected to a laptop via Ethernet and controlled using the Matlab's Instrument Control Toolbox. A tailor-made software controls all the measurement process by means of commands in Standard Commands for Programmable Instruments (SCPI) format using the Virtual Instrument Standard Architecture (VISA) standard and TCP/IP interface.

Various spectrum bands (see Table I) were measured from our department's building at UPC Campus Nord in a urban environment in Barcelona, Spain (latitude: $41^{\circ} 23' 20''$ N; longitude: $2^{\circ} 6' 43''$ E; altitude: 175 meters). Most of the measured bands were analyzed in the selected building's rooftop, which represents a strategic location with direct line-of-sight to several transmitting stations located a few tens or hundreds of meters away from the antenna and without buildings blocking the radio propagation. The measurement equipment was placed inside the building, however, for the DECT and ISM bands since they are used by short-range radio technologies more commonly deployed in indoor environments. These measurement locations were carefully selected in order to maximize the receiving signal-to-noise ratio and hence ensure a reliable and accurate estimation of the true busy/idle states for the channels of the measured bands. Although this work does not present results for all the spectrum bands shown in Table I, the proposed model was developed and validated based on channels from all the measured bands and radio technologies.

Each band was measured across a time span of 7 days, from Monday midnight to Sunday midnight. This measurement period enabled us not only to capture a high number of signal samples (see Table I), but also to appreciate any potential pattern on spectrum use (e.g., channel usage variations between weekdays and weekends as well as variations at different times along days/nights). Measurements were performed using average detection and with a resolution bandwidth of 10 kHz, which allows to resolve signals in frequency even for narrowband technologies such as TETRA and GSM/DCS. The external amplifier shown in Figure 1 along with the spectrum analyzer's internal amplifier (≈ 25 dB gain) result in an overall sensitivity around -130 dBm/10 kHz, which guarantees a reliable estimation of the true spectrum occupancy.

Before validating the proposed model with the captured empirical data, it was first necessary to extract the binary channel occupancy pattern by determining which power samples measured by the spectrum analyzer correspond to busy

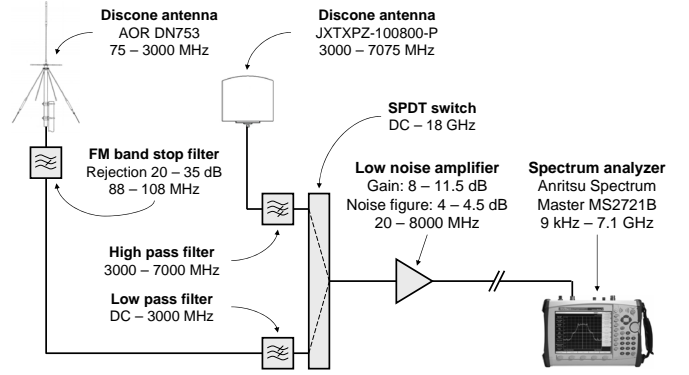


Fig. 1. Measurement setup employed in this study.

TABLE I
SPECTRUM BANDS MEASURED IN THIS WORK.

Measured band	Frequency (MHz)	No. of channels	No. of samples	Avg. sweep time (secs)
TETRA UL	410-420	399	199013	3.04
TETRA DL	420-430	399	195956	3.08
E-GSM 900 UL	880-915	174	156460	3.86
E-GSM 900 DL	925-960	174	158147	3.82
DCS 1800 UL	1710-1785	374	125986	4.80
DCS 1800 DL	1805-1880	374	128615	4.70
DECT	1880-1900	10	178388	3.39
ISM	2400-2500	13	105940	5.70

channels and which others to idle ones. To detect whether a channel is used by a licensed user, a number of different signal detection methods, referred to as *spectrum sensing* algorithms in the context of DSA/CR, have been proposed in the literature [60]–[62]. The existing solutions provide different tradeoffs among required sensing time, complexity and detection capabilities. Their practical applicability, however, depends on how much information is available about the primary user signal. In the most generic case no prior information is available. If only low time-resolution power measurements of the spectrum utilization are available, the application of advanced techniques such as feature detection methods results infeasible and the energy detection method is the only possibility left [63], which is able to work irrespective of the signal to be detected. Due to its simplicity and relevance to the processing of power measurements, energy detection has been a preferred approach for many past spectrum studies and also constitutes the spectrum sensing method considered in this work. Energy detection compares the received signal energy in a certain channel to a properly set decision threshold². If the signal lies above the threshold the channel is declared to be busy (i.e., occupied by the licensed system). Otherwise the channel is supposed to be idle (i.e., available for secondary

²To determine the decision threshold, the antenna of Figure 1 was replaced with a matched load in order to measure the system noise. For each measured channel, the threshold was then set as the maximum noise power measured plus a 3-dB margin to avoid false alarms. On the other hand, the high signal-to-noise ratio conditions under which most of the measured signals were received guarantee that the probability of misdetection is minimized, thus resulting in a nearly ideal detection performance under such conditions.

usage). Following this principle, the power samples measured for each channel were mapped to binary busy/idle states. Based on the resulting binary sequences, the lengths of busy and idle periods were extracted and the proposed DTMC channel model was validated with empirical data.

It is worth noting that the average sweep times shown in Table I indicate that the resulting sampling rates of swept spectrum analyzers as the one employed in this work are not comparable to that of the measurement configurations employed in other modeling studies [44]–[47], which may result in undersampling of the measured signals and thus the misdetection of channel state changes between consecutive channel observations. The binary occupancy pattern observed in such a case, although inaccurate, is still interesting and useful due to two main reasons. The first one is that such binary pattern can be thought of as the occupancy perception of a DSA/CR user that periodically senses the channel and observes its state at discrete time instants. Therefore, spectrum analyzer measurements are useful to model spectrum occupancy from the point of view of the DSA/CR user perception. Since the overall behavior of a DSA/CR network is driven by the primary occupancy pattern as perceived by the sensing nodes, analytical studies and simulations of DSA/CR systems should rely on spectrum use models that are able to accurately capture and reproduce the channel occupancy pattern in real channels as observed by DSA/CR terminals. On the other hand, short idle periods resulting from bursty data transmissions are difficult to exploit for secondary usage in practice³, which from a practical point of view is equivalent to a busy channel state. Exploitable idle periods normally arise when there is no primary user making use of the channel, which can reliably be detected with a spectrum analyzer within reasonable accuracy limits in spite of its limited time resolution. Moreover, it is worth noting that spectrum analyzers have successfully been applied in previous modeling studies [48] and have the advantage of enabling high dynamic ranges, high sensitivities and wideband measurements. The empirical data captured for various radio technologies enabled an adequate validation of the model developed in this work.

A more detailed and in-depth description of the employed measurement setup and its configuration as well as the considered methodological procedures can be found in [64], [65].

IV. DISCRETE-TIME MARKOV CHAIN

At a given time instant, a primary radio channel may be either busy or idle, meaning that the temporal spectrum occupancy pattern of a primary radio channel can adequately be modeled by means of a two-state Markov chain. Let's denote as $\mathbb{S} = \{s_0, s_1\}$ the space state for a primary radio channel, where the s_0 state indicates that the channel is idle and the s_1 state indicates that the channel is busy. The channel state $S(t)$ at time t can either be $S(t) = s_0$ or $S(t) = s_1$. As discussed in Section II, this work focuses on the particular case of DTMCs, where the time index set is discrete, i.e.

³For instance, the time-slot duration is 14.167 ms in TETRA, 577 μ s in GSM/DCS and 417 μ s in DECT. The IEEE 802.11 protocol, used by wireless local area networks operating in the ISM band, defines inter-frame spaces in the order of 50 μ s or less.

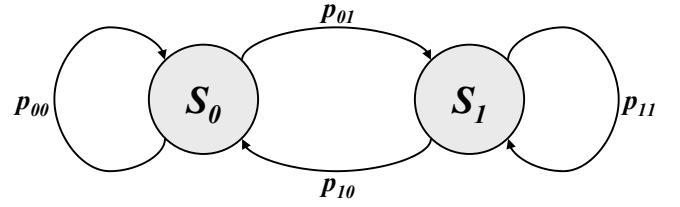


Fig. 2. Discrete-Time Markov Chain (DTMC) model.

$t = t_k = kT_s$, where k is a non-negative integer representing the step number and T_s is the time period between consecutive transitions or state changes⁴. The behavior of a DTMC can be described by means of a set of transition probabilities between states (see Figure 2), which can be expressed in matrix form as:

$$\mathbf{P} = \begin{bmatrix} p_{00} & p_{01} \\ p_{10} & p_{11} \end{bmatrix} \quad (1)$$

where p_{ij} represents the probability that the system transitions from state s_i to state s_j . Note that the channel model commonly used in previous work assumes a stationary (time-homogeneous) DTMC, where the transition matrix \mathbf{P} is constant and independent of the time instant t .

The DC of a channel, henceforth denoted as Ψ , is a very straightforward metric and an accurate reproduction is a minimum requirement for any time-dimension model of spectrum use. The DC can be defined from both probabilistic and empirical perspectives. While the former results more appropriate for theoretical analyses, the latter results more convenient for validation with empirical data. From an empirical viewpoint, the DC can be estimated as the fraction of time that the channel is declared to be busy based on the procedure described in Section III. From a probabilistic viewpoint, the DC can be defined as the probability that the channel is busy. The probabilities that the model of Figure 2 is in each of its states in the long term are given by [66]:

$$P(S = s_0) = \frac{p_{10}}{p_{01} + p_{10}} = 1 - \Psi \quad (2)$$

$$P(S = s_1) = \frac{p_{01}}{p_{01} + p_{10}} = \Psi \quad (3)$$

Thus, the DTMC model can be configured to reproduce any arbitrary DC Ψ by selecting the transition probabilities as $p_{01} = p_{11} = \Psi$ and $p_{10} = p_{00} = 1 - \Psi$, which yields:

$$\mathbf{P} = \begin{bmatrix} 1 - \Psi & \Psi \\ 1 - \Psi & \Psi \end{bmatrix} \quad (4)$$

In order to verify the ability of the DTMC model of equation 4 to reproduce the DC of real channels, the empirical data captured in the measurement campaign were used to estimate the transition probabilities of each channel as:

$$\hat{p}_{ij} = \begin{cases} \frac{\eta_{ij}}{\eta_i}, & \eta_i > 0 \\ 0, & \eta_i = 0 \text{ and } i = j \\ 1, & \eta_i = 0 \text{ and } i \neq j \end{cases} \quad (5)$$

⁴ T_s can be associated to the average sweep times shown in Table I.

where η_{ij} represents the number of transitions from state s_i to s_j occurring in the empirical sequences, and $\eta_i = \sum_{k=0}^{n-1} \eta_{ik}$ is the number of times that the channel resides in state s_i . The two last cases of equation 5 are included in order to account for channels that are always busy ($\Psi = 1$) or always idle ($\Psi = 0$). The theoretical DC corresponding to the estimated probabilities \hat{p}_{ij} was estimated based on equation 3 and compared to the true empirical DC of the channel, appreciating a perfect agreement for channels of all the considered radio technologies. This indicates that the DTMC model of equation 4 is able to accurately reproduce the DC of real channels⁵.

Nevertheless, reproducing not only the DC but also the lengths of the busy and idle periods is an important characteristic of a realistic time-dimension model of spectrum use. While this feature is explicitly represented in the case of CTMC and CTSMC models by means of the sojourn time distributions, there is no mean to account for the state holding times in the case of the DTMC model. Therefore, the DTMC model would not be expected to reproduce the statistical properties of the lengths of busy and idle periods of real channels. To verify this statement, the DTMC channel model was simulated with the transition probabilities \hat{p}_{ij} estimated from empirical data for all the measured channels. During the simulation of the DTMC model, the durations of the state holding times T_i were computed as $T_i = \tilde{\eta}_i \cdot T_s$, where $\tilde{\eta}_i$ represents the number of consecutive steps the channel resides in state s_i during the simulation before switching to the other state, and T_s is the average sweep time corresponding to the considered channel (see Table I). The statistical distributions of busy and idle periods obtained by means of simulation were computed and compared to the empirical distributions of busy and idle periods observed in the measured channels. This comparison was performed for each measured channel of every radio technology. Figures 3–6 show the results obtained for some selected channels. The results are shown in terms of the Complementary Cumulative Distribution Function (CCDF) and with axes in logarithmic scale for a finer detail of accuracy. The time evolution of the DC computed over 1-hour periods is also shown. In general, the obtained results indicate, as expected, that the DTMC channel model is not able to reproduce the statistical properties of the lengths of busy and idle periods of real channels. In some cases, however, the distributions resulting from simulations showed a noticeable agreement with their empirical counterparts (Figure 6 shows an example). After analyzing the empirical data in detail, it was observed that the convergence/divergence of empirical and simulation results can be explained in terms of the channel load variation pattern. When the channel is sparsely used (low load), the length of idle periods is significantly higher than that of busy ones. On the other hand, when the channel is subject to an intensive usage (high load), the length of busy periods increases while idle periods become notably shorter. Since the considered DTMC model is parametrized (i.e., the

transition probabilities are configured) based on the long-term average load of the channel (i.e., the average DC of the whole measurement period), it is not able to capture the channel load variations and, as a result, the DTMC model cannot reproduce the resulting lengths of busy and idle periods. This can clearly be appreciated in Figures 3–5, where the channel load, characterized in terms of the DC, varies with the time and the distributions obtained by simulation diverge from the real ones. The exception, however, corresponds to the case of channels with constant load patterns, where the average DC matches the *instantaneous* DC at all times, and simulation and empirical results then agree as shown in Figure 6.

Since the probabilities of the transition matrix \mathbf{P} depend on the DC Ψ , and Ψ changes over time, this means that the binary occupancy pattern of real channels cannot be modeled, in general, by means of a stationary (time-homogeneous) DTMC⁶ as widely considered in DSA/CR research (see Section II-B). As a result, a non-stationary (time-inhomogeneous) DTMC should be considered, with a time-dependent transition matrix:

$$\mathbf{P}(t) = \begin{bmatrix} 1 - \Psi(t) & \Psi(t) \\ 1 - \Psi(t) & \Psi(t) \end{bmatrix} \quad (6)$$

where $t = t_k = kT_s$ as previously defined.

In the stationary case of equation 4, Ψ represents a constant parameter. However, in the non-stationary case of equation 6, $\Psi(t)$ represents a time-dependent function that needs to be characterized in order to characterize the DTMC channel model in the time domain. Appropriate and accurate DC models for $\Psi(t)$ are therefore required.

The results derived from the empirical data indicated the existence of two well-defined types of channel load variation patterns, namely patterns with an important and remarkably predominant deterministic component (e.g., Figures 3 and 4) and patterns where the carried load appears to vary following a random behavior (e.g., Figure 5). Based on this observation, adequate DC models of $\Psi(t)$ for both cases are developed in Sections V and VI following deterministic and stochastic modeling approaches, respectively.

V. DETERMINISTIC DUTY CYCLE MODEL

In many interesting and important cases, the load variation pattern of primary radio channels is characterized by a predominant deterministic component arising from social behavior and common habits, as it can clearly be appreciated in Figures 3 and 4. These examples correspond to cellular mobile communication systems, namely E-GSM 900 and DCS 1800. Nevertheless, it is interesting to note that similar patterns were also observed in some channels from other radio technologies such as e.g. TETRA. Moreover, deterministic patterns with different shapes were also identified in other cases. This section focuses on the analysis and modeling of the spectrum occupancy patterns commonly observed in cellular mobile communication systems, which are a clear example of predominantly deterministic behaviors. The same modeling

⁵ For CTMC and CTSMC models, any arbitrary DC can also be reproduced by appropriately selecting the parameters of the sojourn time distributions in order to provide mean values $\mathbb{E}\{T_i\}$ such that $\Psi = \mathbb{E}\{T_1\}/(\mathbb{E}\{T_0\} + \mathbb{E}\{T_1\})$ [66], where $\mathbb{E}\{T_0\}$ and $\mathbb{E}\{T_1\}$ are the mean sojourn times in the idle and busy states, respectively.

⁶ A stationary DTMC may be appropriate for a limited time period only if the modeled system shows approximately stationary behavior during this period. Otherwise, a non-stationary DTMC modeling approach is necessary.

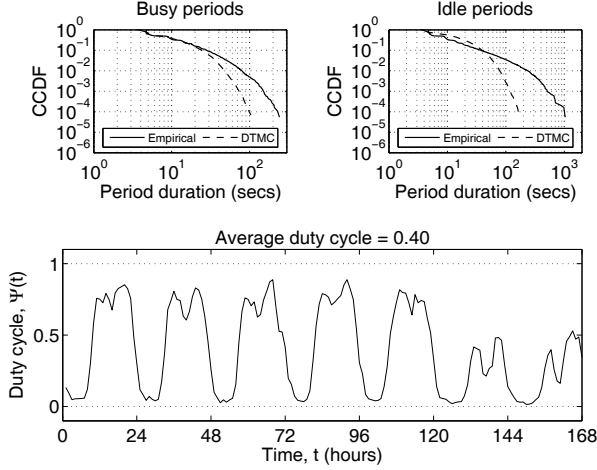


Fig. 3. Empirical and DTMC-simulated distributions of busy and idle periods along with DC time evolution for DCS 1800 DL channel 70.

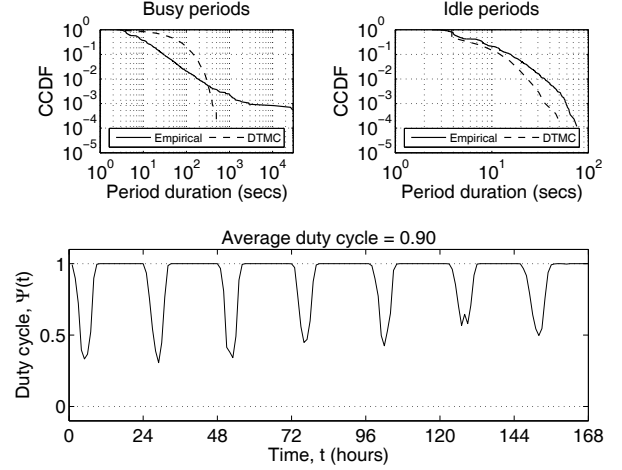


Fig. 4. Empirical and DTMC-simulated distributions of busy and idle periods along with DC time evolution for E-GSM 900 DL channel 23.

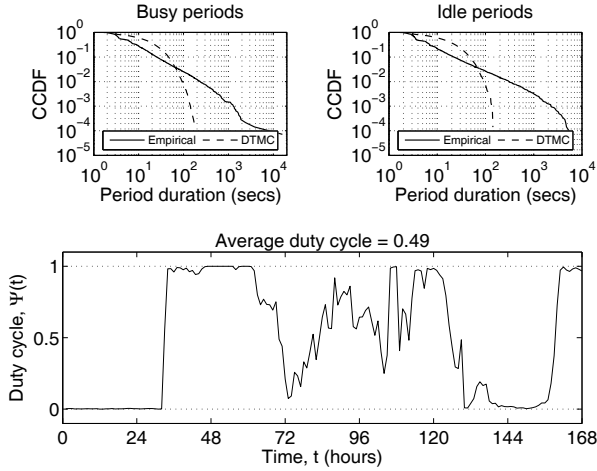


Fig. 5. Empirical and DTMC-simulated distributions of busy and idle periods along with DC time evolution for TETRA DL channel 340.

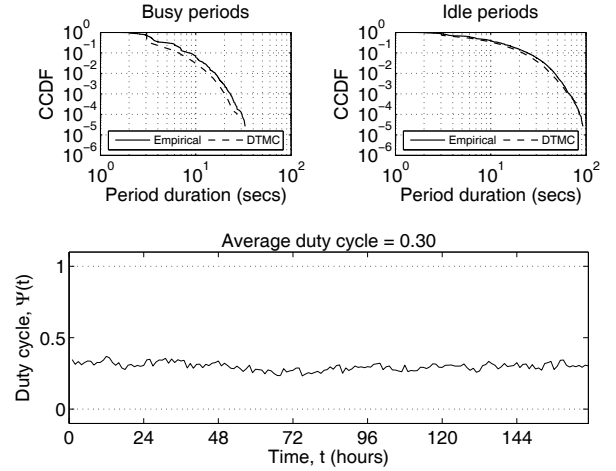


Fig. 6. Empirical and DTMC-simulated distributions of busy and idle periods along with DC time evolution for TETRA UL channel 375.

approach can be used and extended in order to represent other particular patterns that may be found in practice.

The load variation pattern of a cellular system was studied in [67] by means of time series analysis and Auto-Regressive Integrated Moving Average (ARIMA) models. In this section, however, an alternative approach is developed based on the observation that the time evolution of $\Psi(t)$ over time periods of certain length exhibits a clear and predominant deterministic component. Moreover, the analysis of the empirical data corresponding to E-GSM 900 and DCS 1800 indicated that the variation pattern of $\Psi(t)$ is periodic with a period of one day and a slightly different shape between weekdays and weekends due to the lower traffic load normally associated with weekends. Two different shape types for $\Psi(t)$ were identified in the empirical data. The first shape type was normally observed in channels with low/medium loads (average DCs) as in the example of Figure 3, while the second one was more frequently observed in channels with medium/high loads as it is the case of Figure 4. Similar patterns were observed in [68].

A. Deterministic DC Model for Low/Medium Loads

The shape of $\Psi(t)$ in this case can be approximated by the summation of M bell-shaped exponential terms centered at time instants τ_m , with amplitudes A_m and widths σ_m :

$$\Psi(t) \approx \Psi_{min} + \sum_{m=0}^{M-1} A_m e^{-\left(\frac{t-\tau_m}{\sigma_m}\right)^2}, \quad 0 \leq t \leq T \quad (7)$$

where $\Psi_{min} = \min\{\Psi(t)\}$ and T is the time interval over which $\Psi(t)$ is periodic (i.e., one day). The analysis of empirical data indicated that $\Psi(t)$ can accurately be described by means of $M = 3$ terms with τ_1 and τ_2 corresponding to *busy hours* and $\tau_0 = \tau_2 - T$, as illustrated in Figure 7.

Based on empirical results, the approximations $A_0 = A_1 = A_2 = A$ and $\sigma_0 = \sigma_1 = \sigma_2 = \sigma$ are acceptable without incurring in excessive errors, which simplifies the model. Notice that A determines the average value of $\Psi(t)$ in the time interval $[0, T]$, denoted as $\bar{\Psi}$, and it can therefore be expressed

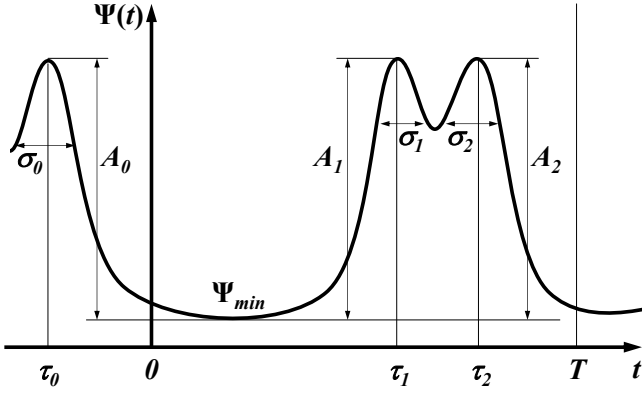


Fig. 7. Parameters of the deterministic DC model for low/medium loads.

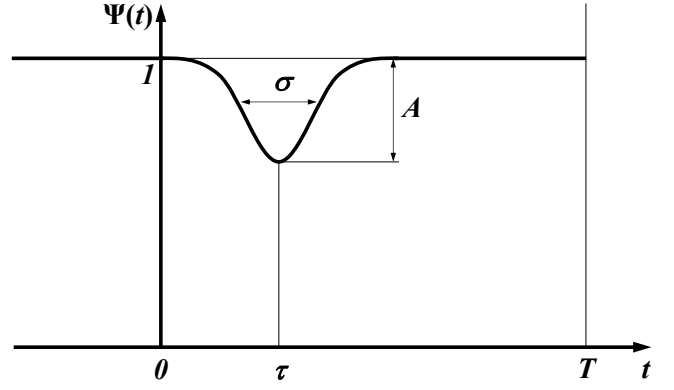


Fig. 8. Parameters of the deterministic DC model for medium/high loads.

as a function of $\bar{\Psi}$ taking into account that:

$$\bar{\Psi} = \frac{1}{T} \int_0^T \Psi(t) dt \approx \Psi_{min} + \frac{A}{T} \sum_{m=0}^{M-1} \int_0^T e^{-\left(\frac{t-\tau_m}{\sigma}\right)^2} dt \quad (8)$$

Solving equation 8 for A and substituting in equation 7 yields:

$$\Psi(t) \approx \Psi_{min} + \frac{2T(\bar{\Psi} - \Psi_{min})}{\sigma\sqrt{\pi}} \cdot \frac{f_{exp}^{l/m}(t, \tau_m, \sigma)}{f_{erf}^{l/m}(T, \tau_m, \sigma)} \quad (9)$$

where $\bar{\Psi} \geq \Psi_{min}$ and:

$$f_{exp}^{l/m}(t, \tau_m, \sigma) = \sum_{m=0}^{M-1} e^{-\left(\frac{t-\tau_m}{\sigma}\right)^2} \quad (10)$$

$$f_{erf}^{l/m}(T, \tau_m, \sigma) = \sum_{m=0}^{M-1} \left[\operatorname{erf}\left(\frac{\tau_m}{\sigma}\right) + \operatorname{erf}\left(\frac{T-\tau_m}{\sigma}\right) \right] \quad (11)$$

Equations 9, 10 and 11 constitute the empirical DC model of $\Psi(t)$ for low/medium loads.

B. Deterministic DC Model for Medium/High Loads

The shape of $\Psi(t)$ in this case can be approximated by an expression based on a single bell-shaped exponential term centered at time instant τ , with amplitude A and width σ :

$$\Psi(t) \approx 1 - Ae^{-\left(\frac{t-\tau}{\sigma}\right)^2}, \quad 0 \leq t \leq T \quad (12)$$

where T is the time interval over which $\Psi(t)$ is periodic (i.e., one day). The model is illustrated in Figure 8, with τ corresponding to the hour with the lowest activity levels.

As in the previous case, A determines the average value of $\Psi(t)$ in the time interval $[0, T]$ and it can therefore be expressed as a function of $\bar{\Psi}$ taking into account that:

$$\bar{\Psi} = \frac{1}{T} \int_0^T \Psi(t) dt \approx 1 - \frac{A}{T} \int_0^T e^{-\left(\frac{t-\tau}{\sigma}\right)^2} dt \quad (13)$$

Solving equation 13 for A and substituting in equation 12 yields:

$$\Psi(t) \approx 1 - \frac{2T(1 - \bar{\Psi})}{\sigma\sqrt{\pi}} \cdot \frac{f_{exp}^{m/h}(t, \tau, \sigma)}{f_{erf}^{m/h}(T, \tau, \sigma)} \quad (14)$$

where:

$$f_{exp}^{m/h}(t, \tau, \sigma) = e^{-\left(\frac{t-\tau}{\sigma}\right)^2} \quad (15)$$

$$f_{erf}^{m/h}(T, \tau, \sigma) = \operatorname{erf}\left(\frac{\tau}{\sigma}\right) + \operatorname{erf}\left(\frac{T-\tau}{\sigma}\right) \quad (16)$$

Equations 14, 15 and 16 constitute the empirical DC model of $\Psi(t)$ for medium/high loads.

C. Deterministic DC Model Validation and Applicability

The objective of this section is to evaluate the ability of the DC models of Sections V-A and V-B to describe the time evolution of $\Psi(t)$ with sufficient accuracy. To this end, the empirical values of $\Psi(t)$ were averaged among 24-hour periods of the same category (i.e., weekdays and weekends) in order to reduce the unavoidable random component of empirical data and extract the deterministic one. The mathematical expressions of equations 9–11 and 14–16 were then fitted to the empirical data by means of curve fitting procedures. The results are shown in Figures 9 and 10, indicating that the proposed DC models are able to accurately reproduce the deterministic component of $\Psi(t)$ in real-world channels.

In order to facilitate to researchers the application of the models in analytical studies as well as in simulations, realistic values of the models' parameters were estimated based on the empirical measurements and by means of curve fitting procedures. The fitted results are shown in Table II. The values are specified in “(minimum; average; maximum)” format. In addition to the models' parameters, the parameter:

$$\kappa = \frac{\bar{\Psi}_{weekends}}{\bar{\Psi}_{weekdays}} \quad (17)$$

has also been included in order to characterize the load level differences observed between weekdays and weekends.

Notice that $\bar{\Psi}$ has not been specified in Table II since this parameter is assumed to be a variable that can be configured in order to reproduce the shape of $\Psi(t)$ with any arbitrary mean $\bar{\Psi}$. Regarding this aspect, it is important to mention that, based on the captured empirical data, it was observed that the DC model for low/medium loads is valid from $\bar{\Psi} = 0$ to $\bar{\Psi} \approx 0.60/0.70$. The maximum $\bar{\Psi}$ for which the model is valid depends on the particular set of selected parameters.

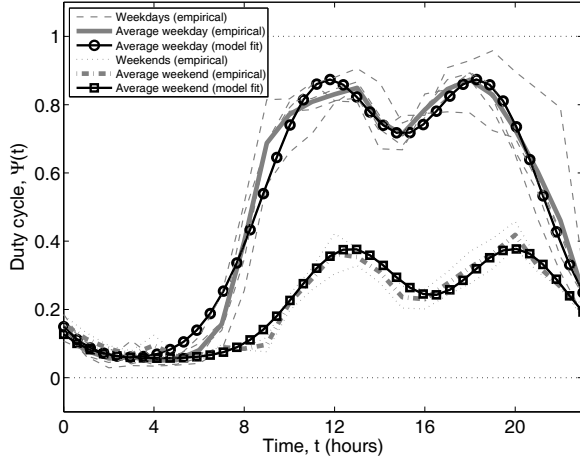


Fig. 9. Validation of the deterministic DC model for low/medium loads.

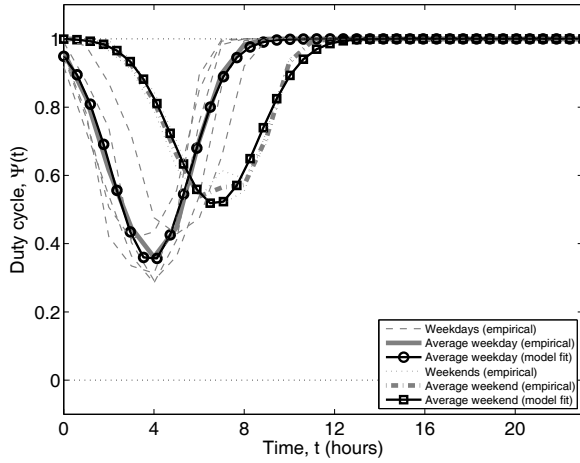


Fig. 10. Validation of the deterministic DC model for medium/high loads.

For the average values of the fitted parameters in Table II, the model is valid up to $\bar{\Psi} = 0.58$ for weekdays and $\bar{\Psi} = 0.55$ for weekends. On the other hand, the DC model for medium/high loads is valid from $\bar{\Psi} \approx 0.46/0.85$ to $\bar{\Psi} = 1$. Again, the minimum $\bar{\Psi}$ for which the model is valid depends on the particular set of selected parameters. For the average values of Table II, the model is valid down to $\bar{\Psi} = 0.80$ for weekdays and $\bar{\Psi} = 0.75$ for weekends. Invalid configurations can readily be identified since in these cases $\Psi(t)$ surpasses the interval $[0, 1]$ within which it must mandatorily be confined.

It is worth noting that the values shown in Table II correspond to empirical measurements performed at a particular location and, as such, are unavoidably affected by the local habits. For example, the usual lunch time in Spain is around 2:00pm and it takes place within a lunch-break of a couple of hours. This schedule may usually be delayed about one hour on weekends. This behavior is indeed clearly appreciated in Figure 9. Habits may be different in other countries (e.g., see Figure 2 of [69] and Figure 4 of [70]), which may result in distinct shapes for $\Psi(t)$. The DC model of equations 9–11 and

TABLE II
FITTED VALUES OF THE DETERMINISTIC DC MODEL PARAMETERS.

Load	Parameter	Weekdays	Weekends
Low/ Med	Ψ_{min}	(0.00; 0.04; 0.31)	(0.00; 0.05; 0.35)
	τ_1 (hours)	(10.74; 11.65; 12.28)	(12.04; 13.03; 14.05)
	τ_2 (hours)	(17.80; 18.99; 20.09)	(19.28; 20.42; 21.54)
	σ (hours)	(3.00; 3.88; 4.31)	(2.49; 3.59; 5.83)
	κ	(0.18; 0.51; 0.82)	
Med/ High	τ (hours)	(2.94; 3.65; 4.08)	(5.64; 6.44; 7.82)
	σ (hours)	(1.99; 2.81; 6.03)	(2.29; 3.41; 8.00)
	κ	(0.69; 0.97; 1.00)	

14–16 can still be valid by fitting the mathematical equations to different empirical data. For instance, an earlier lunch time would result in a lower value of τ_1 while a shorter lunch-break (if any) would result in τ_1 and τ_2 being closer each other. The DC models, nevertheless, would still be valid.

Finally, the DC models of Sections V-A and V-B are envisaged to reproduce the deterministic pattern normally observed in cellular mobile communication systems such as E-GSM 900 and DCS 1800, which may also be present in other systems. Nevertheless, this does not imply that the model is always applicable to such type of systems. For instance, if the system is studied over a relatively short time period (e.g., a few hours), social behavior and external events, which may not be easily predicted, may have significant short-term impact on channel usage. This may cause the deterministic component of $\Psi(t)$ to loss importance with respect to the random one and, as a result, the occupancy of a single channel may experience high and unpredictable variations (e.g., see [71]). In such a case, deterministic DC models may be no longer valid and stochastic modeling approaches, as the one discussed in Section VI, might be a more appropriate alternative.

VI. STOCHASTIC DUTY CYCLE MODEL

The traffic load experienced in a radio channel is normally the consequence of a significant number of random factors such as the number of incoming and outgoing users, the resource management policies employed in the system, and so forth. As a result, the channel usage level, represented by means of $\Psi(t)$, is itself a random variable (see the example of Figure 5). In such a case, a stochastic modeling perspective appears to be a more convenient approach.

The following discussion assumes ergodicity on $\Psi(t)$, meaning that the expected values of its moments, such as its mean and variance, can be estimated as the time averages of the moments, which can be computed from a single sample (i.e., realization) of the process provided that it is sufficiently long. Notice that the sequence of $\Psi(t)$ values empirically derived from the measurements for a given channel represents a single realization of the underlying stochastic process, which is not enough to draw any conclusions on its ergodicity. Nevertheless, as it will be shown later on, the model developed under this assumption results valid and accurate in practice.

In order to determine the statistical properties of the underlying stochastic process based on the captured empirical data, $\Psi(t)$ was obtained for each channel as the time evolution of

the DC computed over periods of various lengths, ranging from a few minutes up to one hour. Assuming ergodicity, the Probability Density Function (PDF) of the underlying stochastic process can be estimated as the empirical PDF resulting from the empirical $\Psi(t)$ values for the considered channel. The empirical PDFs obtained with this procedure were compared to various bounded PDF models. Based on curve fitting procedures, it was found that the empirical PDFs of $\Psi(t)$ can accurately be fitted with the beta distribution [72] and the Kumaraswamy distribution [73], as it can be appreciated in the examples of Figures 11–16. The PDF for the former is given by:

$$f_x^B(x; \alpha, \beta) = \frac{1}{B(\alpha, \beta)} x^{\alpha-1} (1-x)^{\beta-1}, \quad x \in (0, 1) \quad (18)$$

where $\alpha > 0$ and $\beta > 0$ are shape parameters and $B(\alpha, \beta)$ is the beta function given by [74, 6.2.1]:

$$B(\alpha, \beta) = \int_0^1 z^{\alpha-1} (1-z)^{\beta-1} dz \quad (19)$$

while the PDF for the latter is given by:

$$f_x^K(x; a, b) = abx^{a-1} (1-x)^{b-1}, \quad x \in (0, 1) \quad (20)$$

where $a > 0$ and $b > 0$ are shape parameters.

The beta distribution is a well-known and widely used distribution that can be found in many popular software simulation packages, thus facilitating the implementation of the stochastic DC model in simulation tools. However, it might present some difficulties in analytical studies due to the complex expression of its PDF. The Kumaraswamy distribution is similar to the beta distribution, but much simpler to use in analytical studies due to the simpler closed form of its PDF [75]. Therefore, while the former may be more appropriate for simulations, the latter may be more convenient for analytical studies.

Both distributions can be configured to reproduce any arbitrary mean DC, $\bar{\Psi}$, by properly selecting the distribution's parameters. In particular, the mean value of the beta and Kumaraswamy distributions are related with their shape parameters as [72], [73]:

$$\bar{\Psi} = \frac{\alpha}{\alpha + \beta} = bB\left(1 + \frac{1}{a}, b\right) \quad (21)$$

Notice that equation 21 can be satisfied for a given $\bar{\Psi}$ with different combinations of shape parameters α, β and a, b . The particular selection of the shape parameters determines the resulting shape of the distributions. In order to facilitate to researchers the application of the models and their configuration, an exhaustive analysis of the empirical data was performed in order to identify any potential relation between the shape parameters and the resulting channel occupancy pattern in the time domain. Based on such analysis, it was found that the PDF shapes observed in real channels can be classified into six elemental archetypes, each with a characteristic time-domain pattern. Each archetype is defined by its load level (L: low, M: medium, and H: high) as well as its load pattern (type I: very bursty, and type II: moderately bursty, but not constant). The range of shape parameters for each archetype and the corresponding time-domain pattern are (see Figures 11–16):

- Case L.I ($\alpha < 1, \beta \geq 1$): The channel is used ($\Psi(t) > 0$) sporadically and remains unused ($\Psi(t) \approx 0$) most of the time.
- Case L.II ($1 < \alpha < \beta$): The channel is used ($\Psi(t) > 0$) regularly by traffic with low activity factors.
- Case M.I ($\alpha < 1, \beta < 1$): The channel is subject to an intermittent use, where high-load periods are followed by low-load periods in a similar proportion.
- Case M.II ($\alpha > 1, \beta > 1, \alpha \sim \beta$): The channel usage level oscillates weakly around the average level.
- Case H.I ($\alpha \geq 1, \beta < 1$): The channel is used ($\Psi(t) \approx 1$) most of the time, with some periods of lower occupancy levels ($\Psi(t) < 1$).
- Case H.II ($\alpha > \beta > 1$): The channel is not fully used ($\Psi(t) < 1$) but subject to a constant, intensive usage.

The range of values indicated for the parameters of the beta distribution is also valid for the Kumaraswamy distribution by replacing α with a and β with b in type-I cases. In type-II cases, the resulting Kumaraswamy distribution is more difficult to control since the same constraints on a and b may hold for various load levels. Based on the above archetypes and the corresponding range of shape parameters, along with equation 21, the parameters of the models can be configured in order to reproduce not only arbitrary mean load levels but also various occupancy patterns observed in real channels.

VII. MODEL VALIDATION

The aim of this section is to assess the ability of the overall model, composed of the DTMC along with the deterministic and stochastic DC models, to reproduce with sufficient accuracy not only the mean DC of the channel but also the statistical properties of the busy and idle periods.

To this end, the DTMC model of Figure 2 was simulated for a sufficiently high number of iterations (transitions) and at different iterations during the simulation, the transition matrix $\mathbf{P}(t)$ (see equation 6) was updated based on the DC models of Sections V and VI. In the deterministic case, $\Psi(t)$ is computed based on equations 9 and 14, and taking into account the simulation time instant. In the stochastic case, $\Psi(t)$ is drawn from a beta distribution whose parameters are estimated based on the sample mean and sample variance of the empirical $\Psi(t)$. The stationary case widely considered in previous DSA/CR research (see equation 4), where the DC is fixed and equal to the mean value, i.e. $\Psi(t) = \bar{\Psi} \forall t$, was also simulated. The statistical distributions obtained in both cases were compared to the real ones derived from empirical data. The obtained results are shown in Figures 17–19.

As it can be appreciated in Figures 17 and 18, the deterministic DC models are able to closely follow and reproduce the deterministic component of $\Psi(t)$ in the time domain and, as a result, the overall model is able to reproduce not only the mean DC of the channel, $\bar{\Psi}$, but also the statistical properties of busy and idle periods, which does not occur with the stationary case where the DTMC is simulated without appropriate DC models.

In the case of the stochastic DC model, the generated sequence of $\Psi(t)$ values does not follow the empirical $\Psi(t)$ values of the channel in the time domain, as it can be

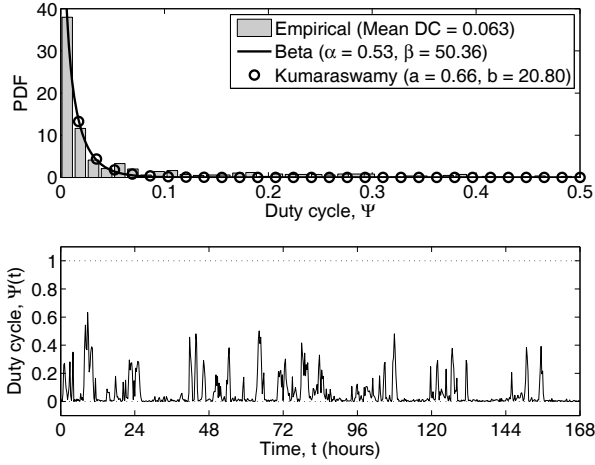


Fig. 11. Stochastic DC models: case L.I.

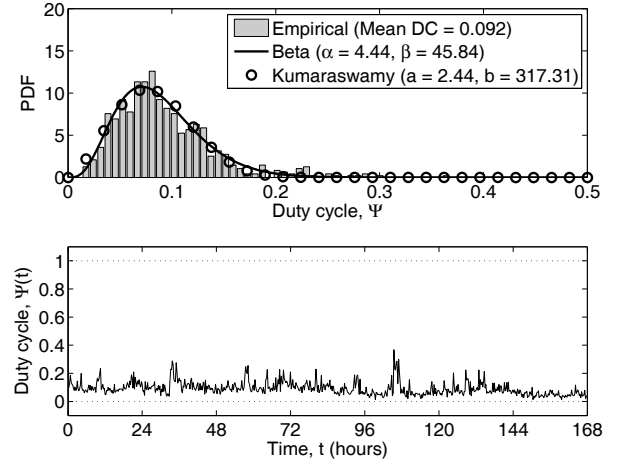


Fig. 14. Stochastic DC models: case L.II.

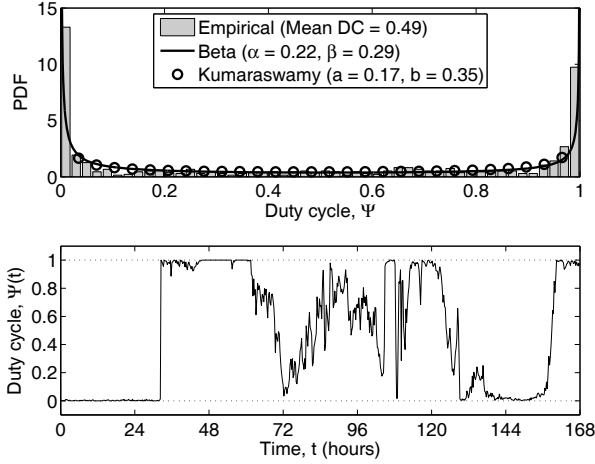


Fig. 12. Stochastic DC models: case M.I.

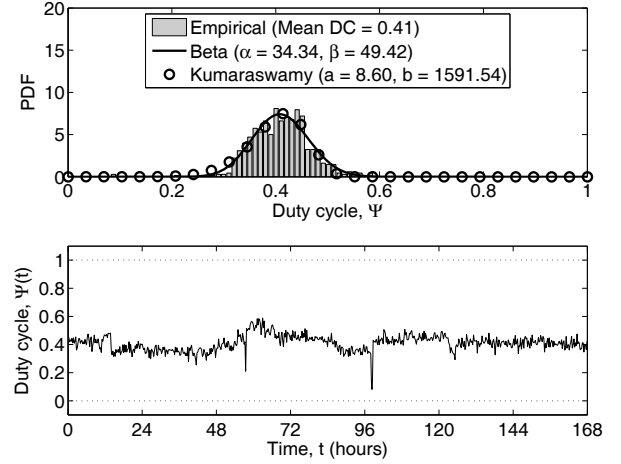


Fig. 15. Stochastic DC models: case M.II.

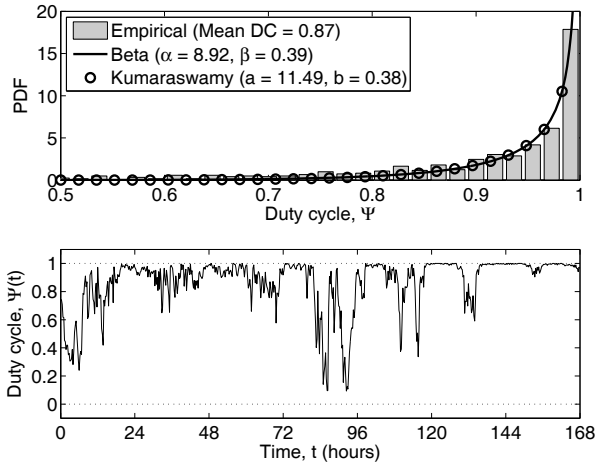


Fig. 13. Stochastic DC models: case H.I.

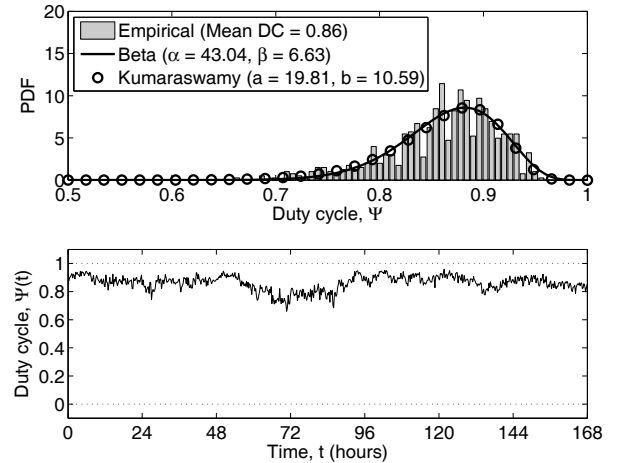


Fig. 16. Stochastic DC models: case H.II.

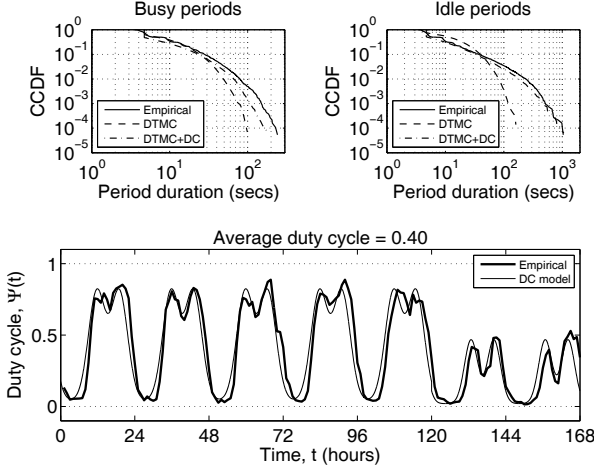


Fig. 17. Empirical and DTMC-simulated distributions of busy and idle periods along with DC time evolution for DCS 1800 DL channel 70.

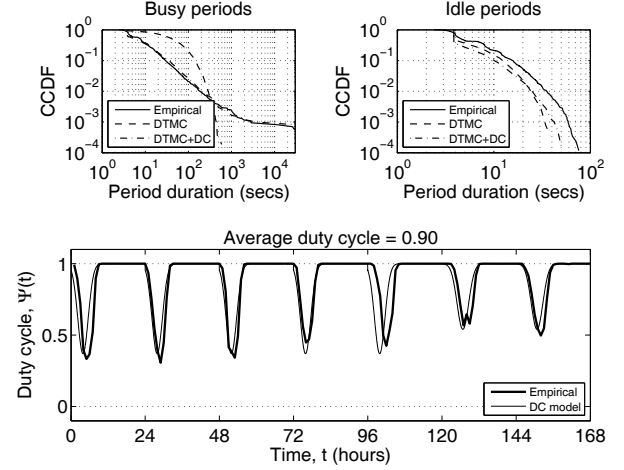


Fig. 18. Empirical and DTMC-simulated distributions of busy and idle periods along with DC time evolution for E-GSM 900 DL channel 23.

appreciated in Figure 19. However, it is important to note that the stochastic approach is not aimed at reproducing the time evolution of a particular realization of the stochastic process $\Psi(t)$, but the statistical properties thereof. The results shown in Figure 19 demonstrate that this modeling approach is also a valid and significantly accurate alternative to reproduce the statistical properties of busy and idle periods of real channels.

Taking into account the logarithmic axes representation of Figures 17–19, it can be appreciated that the distributions of busy and idle periods are reproduced with a significant level of precision. In order to objectively assess the accuracy, the Kolmogorov-Smirnov (KS) test [76] was performed over the obtained simulation results in order to compute the KS distances $D_{KS}(T_0)$ and $D_{KS}(T_1)$, for idle and busy periods respectively, between the empirical distribution functions and the corresponding counterparts obtained by means of simulation. Such study indicated that $D_{KS}(T_0) = 0.08$ and $D_{KS}(T_1) = 0.09$ (Figure 17), $D_{KS}(T_0) = 0.13$ and $D_{KS}(T_1) = 0.06$ (Figure 18), while $D_{KS}(T_0) = 0.06$ and $D_{KS}(T_1) = 0.09$ (Figure 19), which highlights the remarkably good accuracy of the proposed modeling approach.

Before concluding this section, it is worth noting that the practical implementation of the stochastic DC model in simulation tools may not lead to accurate results if some observations are not carefully taken into account. In particular, the DTMC has to be iterated a sufficient number of times, N , before updating $\mathbf{P}(t)$ according to the stochastic DC model. During such amount of iterations, the transition probabilities of the DTMC must remain unaltered. After such N iterations, a new value of $\Psi(t)$ can be generated from a beta or Kumaraswamy distribution, and used to update the transition matrix $\mathbf{P}(t)$ for the next N iterations. If the transition matrix is updated excessively fast (e.g., every iteration) the overall model may not be able to accurately reproduce the lengths of busy and idle periods.

In conclusion, the obtained results demonstrate that the non-stationary DTMC model along with the proposed deterministic and stochastic DC models is able to accurately reproduce not

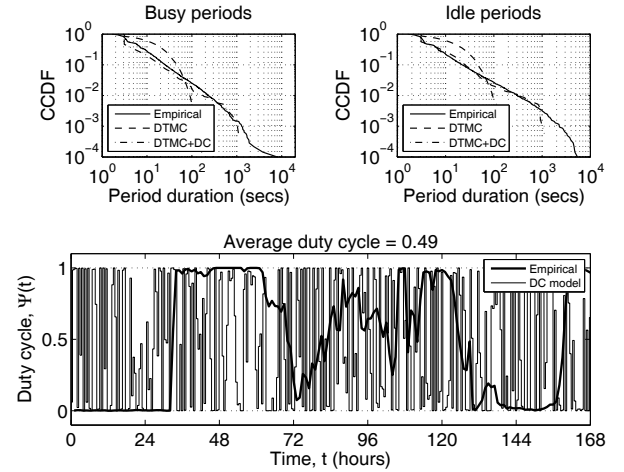


Fig. 19. Empirical and DTMC-simulated distributions of busy and idle periods along with DC time evolution for TETRA DL channel 340.

only the mean occupancy but also the statistical properties of busy and idle periods observed in real channels.

VIII. CASE STUDY

The aim of this section is to demonstrate and illustrate the importance of employing realistic and accurate spectrum occupancy models in the design and evaluation of DSA/CR techniques. To this end, this section considers a simple medium access scheme where a CR terminal senses a primary radio channel periodically and accesses the channel whenever it is sensed as idle. Although the case study of this section may be considered to be trivial, it will suffice to illustrate the impact of the realism and accuracy of spectrum occupancy models on the design and performance evaluation of more sophisticated solutions such as adaptive spectrum sensing techniques, MAC protocols, MAC-layer sensing schemes, dynamic channel selection algorithms and opportunistic scheduling policies.

Let's assume that the CR terminal senses and accesses the channel on a frame basis as illustrated in Figure 20. Each frame is composed of K slots with duration T_s . The CR

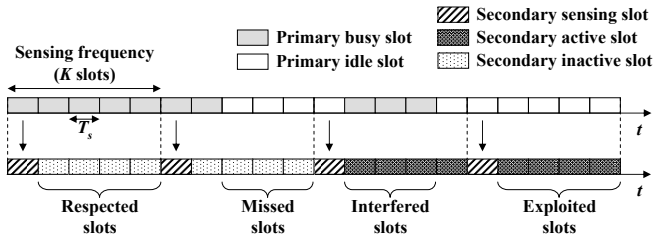


Fig. 20. Case study description.

terminal senses the channel in the first slot of the frame and decides to transmit or not in the following $K - 1$ slots based on the sensing result (perfect sensing is assumed). If the CR terminal senses the channel as busy and decides not to transmit, the following slots may be classified as *respected slots* if the primary user transmits in such slots, or *missed slots* otherwise. On the other hand, a secondary transmission may result in *interfered slots* if the primary is also active, or *exploited slots* otherwise, as illustrated in Figure 20.

The objective is to evaluate the performance of the considered medium access scheme when the sequence of channel occupancy states corresponds to: a) empirical measurements of real channels, b) occupancy sequences generated with the non-stationary DTMC model along with DC models, and c) occupancy sequences generated with the stationary DTMC model alone. The comparison of the results obtained in these cases will provide a quantitative illustration of the consequences of considering (un)realistic and (in)accurate spectrum occupancy models in DSA/CR research.

Table III shows the channel access statistics obtained for the above mentioned sequences of channel occupancy states in the case of a DECT channel. As it can be appreciated, the proposed non-stationary approach (labeled as “DTMC+DC”) is able to provide accurate estimations of the true channel use statistics. The results provided by the stationary approach (labeled as “DTMC”), although less accurate, can be considered acceptable as well. This can be explained by the fact that the considered metrics represent the average number of slots for each type in the long term. As such, they depend on the average number of busy/idle slots or, in other words, the average DC of the channel. Since both DTMC modeling alternatives (stationary and non-stationary) are able to accurately reproduce the channel’s average DC, the obtained average values for the considered metrics agree in both cases with the empirical, real ones. However, it is worth noting that in M.I-type channels (referring to the nomenclature used in Section VI), the stationary DTMC model was observed to fail in providing acceptable results while the proposed non-stationary DTMC model was still able to do so, as illustrated in Table IV. Therefore, although the stationary DTMC model is able to reproduce the true mean DC value of the channel, this does not guarantee the reliability of average performance metrics obtained when applying such model. On the other hand, the proposed non-stationary DTMC approach provides accurate estimates of average performance metrics.

The average value of performance metrics, although useful, may not provide a full impression on the real performance of

TABLE III
CHANNEL ACCESS STATISTICS FOR DECT CHANNEL 9 (STOCHASTIC DC MODEL AND $K = 5$)

Slot type	Empirical	DTMC+DC	DTMC
Respected	2.67%	2.75%	1.16%
Missed	8.34%	8.31%	9.95%
Interfered	8.25%	8.30%	9.73%
Exploited	80.74%	80.64%	79.16%

TABLE IV
CHANNEL ACCESS STATISTICS FOR TETRA DL CHANNEL 340
(STOCHASTIC DC MODEL AND $K = 5$)

Slot type	Empirical	DTMC+DC	DTMC
Respected	41.37%	41.15%	23.84%
Missed	7.39%	7.23%	25.25%
Interfered	7.20%	7.81%	24.72%
Exploited	44.04%	43.81%	26.19%

a DSA/CR technique under study. For example, let’s assume that a primary user tolerates a short communication disruption provided that its duration is below a given threshold δ_d . In such a case, the probability that the duration of interference periods exceeds δ_d would be a more useful performance metric than the average number of interfered slots. As shown in Figure 21, the distribution of interference periods resulting from the medium access technique under study is accurately reproduced by the proposed non-stationary DTMC modeling approach, which is not the case of the stationary DTMC model. As a result, the real interference to a primary user is accurately estimated with the former, while it is significantly underestimated with the latter. Concretely, while the application of the stationary DTMC model results in errors up to 9% in the predicted interference probability, the prediction provided by the proposed non-stationary DTMC model is around 1% below the real value obtained from the real channel occupancy pattern. Therefore, even when the stationary DTMC approach is able to provide accurate estimates of average metrics, it fails in providing acceptable results for other more sophisticated performance metrics. These results demonstrate and highlight the importance of employing realistic and accurate spectrum occupancy models, as the one proposed in this work, for the design and performance evaluation of DSA/CR techniques.

IX. CONCLUSIONS

Due to the opportunistic nature of the DSA/CR principle, the behavior and performance of a secondary network depends on the spectrum occupancy patterns of the primary system. A realistic and accurate modeling of such patterns becomes therefore essential. This work has demonstrated that the stationary DTMC model widely used in the DSA/CR literature in order to describe the binary occupancy pattern of primary channels in the time domain is not able to reproduce relevant properties of spectrum use. As a result, a non-stationary DTMC model with deterministic and stochastic DC models has been developed. The proposed approach has been validated with extensive empirical measurement results,

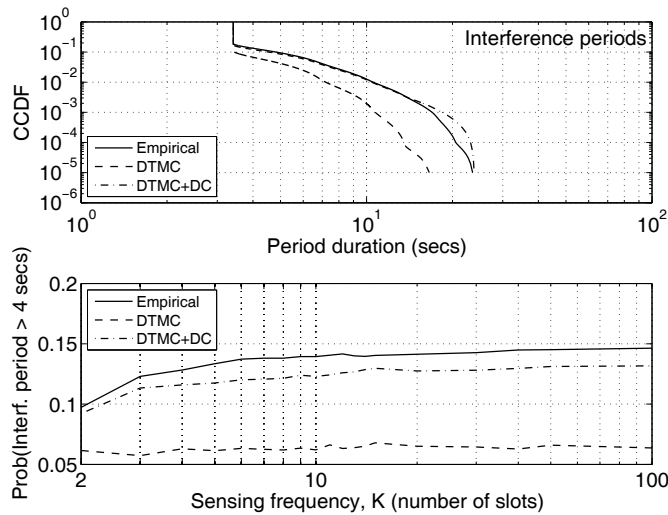


Fig. 21. Interference results for DECT channel 9. Upper graph: distribution of interference periods ($K = 5$). Lower graph: Probability of interference as a function of the sensing frequency ($\delta_d = 4$ secs).

demonstrating that it is able to accurately reproduce not only the mean occupancy level but also the statistical properties of busy and idle periods observed in real-world channels. The importance of realistically and accurately modeling spectrum use in the design and evaluation of DSA/CR techniques has been highlighted with a practical case study.

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